

Un programme à mots plus courts pour connaître la primalité des entiers

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On fournit simplement ici une petite adaptation d'un programme fourni précédemment et tel qu'un nombre est premier si son mot de Christoffel sous une portion d'hyperbole est égal au mot de son successeur.

```
1 #include <iostream>
2 #include <stdio.h>
3
4 int main(int argc, char* argv[]) {
5     int n, i, xcourant, ycourant, xa, xb ;
6     float res ;
7
8     for (n = 3 ; n <= 100 ; ++n) {
9         printf("%5d == ", n) ;
10        xcourant = 1 ; if (n%2 == 0) ycourant = n/2-1 ; else ycourant = n/2 ;
11        xa = 0 ; xb = 0 ;
12        for (i = n/2+1 ; i <= n-2 ; ++i) {
13            res = n-((xcourant + 1) * ycourant) ;
14            if (res > 0) {
15                if (i > n/2+1) std::cout << "b" ;
16                xcourant = xcourant+1 ;
17                xa = 0 ; xb = xb+1 ;
18            }
19            else {
20                if (i > n/2+1) std::cout << "a" ;
21                ycourant = ycourant-1 ;
22                xb = 0 ; xa = xa+1 ;
23            }
24        }
25        std::cout << "\n" ;
26    }
27 }
```

Ci-dessous, les mots calculés par ce programme :

```

1   7 == a
2   8 == a
3   9 == aa
4   10 == ab
5   11 == aab
6   12 == aab
7   13 == aaba
8   14 == aaba
9   15 == aaaba
10  16 == aabaa
11  17 == aaabab
12  18 == aaabab
13  19 == aaabaab
14  20 == aaaabaab
15  21 == aaaababa
16  22 == aaabaaba
17  23 == aaaabaaba
18  24 == aaaabaaba
19  25 == aaaabaabaa
20  26 == aaaabaabab
21  27 == aaaaabaabab
22  28 == aaaaabaaabab
23  29 == aaaaabaabaab
24  30 == aaaaabaabaab
25  31 == aaaaabaababa
26  32 == aaaaabaaababa
27  33 == aaaaaabaabaaba
28  34 == aaaaabaabaaba
29  35 == aaaaaabaabaaba
30  36 == aaaaaabaaababaa
31  37 == aaaaaabaaabaabab
32  38 == aaaaaabaaabaabab
33  39 == aaaaaaabaaabaabab
34  40 == aaaaaabaaaabaabab
35  41 == aaaaaaabaaaabaabab
36  42 == aaaaaaabaaaabaabab
37  43 == aaaaaaabaaaabaababa
38  44 == aaaaaaabaaaabaababa
39  45 == aaaaaaabaaaabaababa
40  46 == aaaaaaabaaaabaababa
41  47 == aaaaaaabaaaabaababa
42  48 == aaaaaaabaaaabaababa
43  49 == aaaaaaabaaaabaaaababaa
44  50 == aaaaaaabaaaabaaaababab
45  51 == aaaaaaaaaabaaaabaabab
46  52 == aaaaaaaaaabaaaaabaabab
47  53 == aaaaaaaaaabaaaabaabab
48  54 == aaaaaaaaaabaaaabaabab
49  55 == aaaaaaaaaabaaaabaaaabab
50  56 == aaaaaaaaaabaaaabaaaabab
51  57 == aaaaaaaaaabaaaabaaaabab
52  58 == aaaaaaaaaabaaaabaaaabab
53  59 == aaaaaaaaaabaaaabaaaabab
54  60 == aaaaaaaaaabaaaabaaaabab
55  61 == aaaaaaaaaabaaaabaaaabab
56  62 == aaaaaaaaaabaaaabaaaabab
57  63 == aaaaaaaaaabaaaabaaaabab
58  64 == aaaaaaaaaabaaaabaaaabab
59  65 == aaaaaaaaaabaaaabaaaabab
60  66 == aaaaaaaaaabaaaabaaaabab
61  67 == aaaaaaaaaabaaaabaaaabab
62  68 == aaaaaaaaaabaaaabaaaabab
63  69 == aaaaaaaaaabaaaabaaaabab
64  70 == aaaaaaaaaabaaaabaaaabab

```

```
1 71 == aaaaaaaaaaaaaabaaaaabaaababaab
2 72 == aaaaaaaaaaaaaabaaaaabaaabaaababaab
3 73 == aaaaaaaaaaaaaabaaaaabaaaabaababa
4 74 == aaaaaaaaaaaaaabaaaaabaaaabaabaababa
5 75 == aaaaaaaaaaaaaabaaaaabaaaabaabaababa
6 76 == aaaaaaaaaaaaaabaaaaabaaaabaababa
7 77 == aaaaaaaaaaaaaabaaaaabaaaabaababa
8 78 == aaaaaaaaaaaaaabaaaaabaaaabaababa
9 79 == aaaaaaaaaaaaaabaaaaabaaaabaababa
10 80 == aaaaaaaaaaaaaabaaaaabaaaabaababa
11 81 == aaaaaaaaaaaaaabaaaaabaaaabaababaa
12 82 == aaaaaaaaaaaaaabaaaaabaaaabaababab
13 83 == aaaaaaaaaaaaaabaaaaabaaaabaababab
14 84 == aaaaaaaaaaaaaabaaaaabaaaabaababab
15 85 == aaaaaaaaaaaaaabaaaaabaaaabaababab
16 86 == aaaaaaaaaaaaaabaaaaabaaaabaababab
17 87 == aaaaaaaaaaaaaabaaaaabaaaabaababab
18 88 == aaaaaaaaaaaaaabaaaaabaaaabaababab
19 89 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
20 90 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
21 91 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
22 92 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
23 93 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
24 94 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
25 95 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
26 96 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
27 97 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
28 98 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
29 99 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
30 100 == aaaaaaaaaaaaaabaaaaabaaaabaaababab
```