

Even numbers'Goldbach components are systematically indicated within parentheses after the even number considered, preceded by the letters *GC*.

## 1 Even numbers of the form $n = 6m$ from 144 to 30

The double sieve of Eratosthenes application is presented in a table in which  $\lfloor \frac{n}{12} \rfloor$  numbers of the top part belong to the arithmetic progression  $6k - 1$  while  $\lfloor \frac{n-6}{12} \rfloor$  numbers of the bottom part belong to the arithmetic progression  $6k + 1$ .

We note in the second column the result of the first pass of the sieve (elimination of numbers that are congruent to 0 according to a modulus smaller than or equal to  $\sqrt{n}$ , to find prime numbers between  $\sqrt{n}$  and  $n/2$ ).

We note in the third column result of the second pass of the sieve by specifying the shared congruence with  $n$  (to find numbers whose complementary to  $n$  is prime).

All modules smaller than  $\sqrt{n}$  except those of  $n$ 's euclidean decomposition appear in third column (for modules that divide  $n$ , first and second pass eliminate same numbers).

The same module can't be found on the same line in second and third column.

- $n = 144$  (*GC* : 5, 7, 13, 17, 31, 37, 41, 43, 47, 61, 71)  
 $n = 2^4 \cdot 3^2$ .  
 $n/2 = 72$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 4 \pmod{5}, n \equiv 4 \pmod{7}, n \equiv 1 \pmod{11}$ .

5 ( <i>p</i> )	0 ( <i>mod</i> 5)		139 ( <i>p</i> )	
11 ( <i>p</i> )	0 ( <i>mod</i> 11)	4 ( <i>mod</i> 7)	133	
17 ( <i>p</i> )			127 ( <i>p</i> )	17 + 127
23 ( <i>p</i> )		1 ( <i>mod</i> 11)	121	
29 ( <i>p</i> )		4 ( <i>mod</i> 5)	115	
35	0 ( <i>mod</i> 5) and 0 ( <i>mod</i> 7)		109 ( <i>p</i> )	
41 ( <i>p</i> )			103 ( <i>p</i> )	41 + 103
47 ( <i>p</i> )			97 ( <i>p</i> )	47 + 97
53 ( <i>p</i> )		4 ( <i>mod</i> 7)	91	
59 ( <i>p</i> )		4 ( <i>mod</i> 5)	85	
65	0 ( <i>mod</i> 5)		79 ( <i>p</i> )	
71 ( <i>p</i> )			73 ( <i>p</i> )	71 + 73
7 ( <i>p</i> )	0 ( <i>mod</i> 7)		137 ( <i>p</i> )	
13 ( <i>p</i> )			131 ( <i>p</i> )	13 + 131
19 ( <i>p</i> )		4 ( <i>mod</i> 5)	125	
25	0 ( <i>mod</i> 5)	4 ( <i>mod</i> 7)	119	
31 ( <i>p</i> )			113 ( <i>p</i> )	31 + 113
37 ( <i>p</i> )			107 ( <i>p</i> )	37 + 107
43 ( <i>p</i> )			101 ( <i>p</i> )	43 + 101
49	0 ( <i>mod</i> 7)	4 ( <i>mod</i> 5)	95	
55	0 ( <i>mod</i> 5) and 0 ( <i>mod</i> 11)		89 ( <i>p</i> )	
61 ( <i>p</i> )			83 ( <i>p</i> )	61 + 83
67 ( <i>p</i> )		4 ( <i>mod</i> 7) and 1 ( <i>mod</i> 11)	77	

- $n = 138$  (GC : 7, 11, 29, 31, 37, 41, 59, 67)  
 $n = 2 \cdot 3 \cdot 23$ .  
 $n/2 = 69$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 3 \pmod{5}, n \equiv 5 \pmod{7}, n \equiv 6 \pmod{11}$ .

5 (p)	0 (mod 5)	5 (mod 7)	133	
11 (p)	0 (mod 11)		127 (p)	
17 (p)		6 (mod 11)	121	
23 (p)		3 (mod 5)	115	
29 (p)			109 (p)	29 + 109
35	0 (mod 5) and 0 (mod 7)		103 (p)	
41 (p)			97 (p)	41 + 97
47 (p)		5 (mod 7)	91	
53 (p)		3 (mod 5)	85	
59			79 (p)	59 + 79
65	0 (mod 5)		73 (p)	
7 (p)	0 (mod 7)		131 (p)	
13 (p)		3 (mod 5)	125	
19 (p)		5 (mod 7)	119	
25	0 (mod 5)		113 (p)	
31 (p)			107 (p)	31 + 107
37 (p)			101 (p)	37 + 101
43 (p)		3 (mod 5)	95	
49	0 (mod 7)		89 (p)	
55	0 (mod 5) and 0 (mod 11)		83 (p)	
61 (p)		5 (mod 7) and 6 (mod 11)	77	
67			71 (p)	67 + 71

- $n = 132$  (GC : 5, 19, 23, 29, 31, 43, 53, 59, 61)  
 $n = 2^2 \cdot 3 \cdot 11$ .  
 $n/2 = 66$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 2 \pmod{5}, n \equiv 6 \pmod{7}, n \equiv 0 \pmod{11}$ .

5 (p)	0 (mod 5)		127 (p)	
11 (p)	0 (mod 11)		121	
17 (p)		2 (mod 5)	115	
23 (p)			109 (p)	23 + 109
29 (p)			103 (p)	29 + 103
35	0 (mod 5) and 0 (mod 7)		97 (p)	
41 (p)		6 (mod 7)	91	
47 (p)		2 (mod 5)	85	
53 (p)			79 (p)	53 + 79
59 (p)			73 (p)	59 + 73
65	0 (mod 5)		67 (p)	
7 (p)	0 (mod 7)	2 (mod 5)	125	
13 (p)		6 (mod 7)	119	
19 (p)			113 (p)	19 + 113
25	0 (mod 5)		107 (p)	
31 (p)			101 (p)	31 + 101
37 (p)		2 (mod 5)	95	
43 (p)			89 (p)	43 + 89
49	0 (mod 7)		83 (p)	
55	0 (mod 5) and 0 (mod 11)		77	
61 (p)			71 (p)	61 + 71

- $n = 126$  ( $DG : 13, 17, 19, 23, 29, 37, 43, 47, 53, 59$ )  
 $n = 2 \cdot 3^2 \cdot 7$ .  
 $n/2 = 63$ .  
 $11 < \sqrt{n} < 13$ . Les modules à considérer sont 5, 7 and 11.  
 $n \equiv 1 \pmod{5}, n \equiv 0 \pmod{7}, n \equiv 5 \pmod{11}$ .

5 ( $p$ )	0 ( $\text{mod } 5$ )	5 ( $\text{mod } 11$ )	121	
11 ( $p$ )	0 ( $\text{mod } 11$ )	1 ( $\text{mod } 5$ )	115	
17 ( $p$ )			109 ( $p$ )	17 + 109
23 ( $p$ )			103 ( $p$ )	23 + 103
29 ( $p$ )			97 ( $p$ )	29 + 97
35	0 ( $\text{mod } 5$ ) and 0 ( $\text{mod } 7$ )		91	
41 ( $p$ )		1 ( $\text{mod } 5$ )	85	
47 ( $p$ )			79 ( $p$ )	47 + 79
53 ( $p$ )			73 ( $p$ )	53 + 73
59 ( $p$ )			67 ( $p$ )	59 + 67
7 ( $p$ )	0 ( $\text{mod } 7$ )		119	
13 ( $p$ )			113 ( $p$ )	13 + 113
19 ( $p$ )			107 ( $p$ )	19 + 107
25	0 ( $\text{mod } 5$ )		101 ( $p$ )	
31 ( $p$ )		1 ( $\text{mod } 5$ )	95	
37 ( $p$ )			89 ( $p$ )	37 + 89
43 ( $p$ )			83 ( $p$ )	43 + 83
49	0 ( $\text{mod } 7$ )	5 ( $\text{mod } 11$ )	77	
55	0 ( $\text{mod } 5$ ) and 0 ( $\text{mod } 11$ )		71 ( $p$ )	
61 ( $p$ )		1 ( $\text{mod } 5$ )	65	

- $n = 120$  ( $GC : 7, 11, 13, 17, 19, 23, 31, 37, 41, 47, 53, 59$ )  
 $n = 2^3 \cdot 3 \cdot 5$ .  
 $n/2 = 60$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 1 \pmod{7}$ .

5 ( $p$ )	0 ( $\text{mod } 5$ )		115	
11 ( $p$ )			109 ( $p$ )	11 + 109
17 ( $p$ )			103 ( $p$ )	17 + 103
23 ( $p$ )			97 ( $p$ )	23 + 97
29 ( $p$ )		1 ( $\text{mod } 7$ )	91	
35	0 ( $\text{mod } 5$ ) and 0 ( $\text{mod } 7$ )		85	
41 ( $p$ )			79 ( $p$ )	41 + 79
47 ( $p$ )			73 ( $p$ )	47 + 73
53 ( $p$ )			67 ( $p$ )	53 + 67
59 ( $p$ )			61 ( $p$ )	59 + 61
7 ( $p$ )	0 ( $\text{mod } 7$ )		103 ( $p$ )	
13 ( $p$ )			97 ( $p$ )	13 + 97
19 ( $p$ )			91 ( $p$ )	19 + 91
25	0 ( $\text{mod } 5$ )		85	
31 ( $p$ )			79 ( $p$ )	31 + 79
37 ( $p$ )			73 ( $p$ )	37 + 73
43 ( $p$ )		1 ( $\text{mod } 7$ )	67 ( $p$ )	
49	0 ( $\text{mod } 7$ )		61 ( $p$ )	
55	0 ( $\text{mod } 5$ ) and 0 ( $\text{mod } 11$ )		55	

- $n = 114$  ( $GC : 5, 7, 11, 13, 17, 31, 41, 43, 47, 53$ )  
 $n = 2 \cdot 3 \cdot 19$ .  
 $n/2 = 57$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 4 \pmod{5}, n \equiv 2 \pmod{7}$ .

5 (p)	0 (mod 5)		109 (p)	
11 (p)			103 (p)	11 + 103
17 (p)			97 (p)	17 + 97
23 (p)		2 (mod 7)	91	
29 (p)		4 (mod 5)	85	
35	0 (mod 5) and 0 (mod 7)		79 (p)	
41 (p)			73 (p)	41 + 73
47 (p)			67 (p)	47 + 67
53 (p)			61 (p)	53 + 61
7 (p)	0 (mod 7)		107 (p)	
13 (p)			101 (p)	13 + 101
19 (p)		4 (mod 5)	95	
25	0 (mod 5)		89 (p)	
31 (p)			83 (p)	31 + 83
37 (p)		2 (mod 7)	77	
43 (p)			71 (p)	43 + 71
49	0 (mod 7)	4 (mod 5)	65	
55	0 (mod 5) and 0 (mod 11)		59 (p)	

- $n = 108$  ( $GC : 5, 7, 11, 19, 29, 37, 41, 47$ )  
 $n = 2^2 \cdot 3^3$ .  
 $n/2 = 54$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 3 \pmod{7}$ .

5 (p)	0 (mod 5)		103 (p)	
11 (p)			97 (p)	11 + 97
17 (p)		3 (mod 7)	91	
23 (p)		3 (mod 5)	85	
29 (p)			79 (p)	29 + 79
35	0 (mod 5) and 0 (mod 7)		73 (p)	
41 (p)			67 (p)	41 + 67
47 (p)			61 (p)	47 + 61
53 (p)		3 (mod 5)	55	
7 (p)	0 (mod 7)		101 (p)	
13 (p)		3 (mod 5)	95	
19 (p)			89 (p)	19 + 89
25	0 (mod 5)		83 (p)	
31 (p)		3 (mod 7)	77	
37 (p)			71 (p)	37 + 71
43 (p)		3 (mod 5)	65	
49	0 (mod 7)		59 (p)	

- $n = 102$  ( $GC : 5, 13, 19, 23, 29, 31, 41, 43$ )

$$n = 2 \cdot 3 \cdot 17.$$

$$n/2 = 51.$$

$7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.

$$n \equiv 2 \pmod{5}, n \equiv 4 \pmod{7}.$$

5 (p)	0 (mod 5)		97 (p)	
11 (p)		4 (mod 7)	91	
17 (p)		2 (mod 5)	85	
23 (p)			79 (p)	23 + 79
29 (p)			73 (p)	29 + 73
35	0 (mod 5) and 0 (mod 7)		67 (p)	
41 (p)			61 (p)	41 + 61
47 (p)		2 (mod 5)	55	
7 (p)	0 (mod 7)	2 (mod 5)	95	
13 (p)			89 (p)	13 + 89
19 (p)			83 (p)	19 + 83
25	0 (mod 5)	4 (mod 7)	77	
31 (p)			71 (p)	31 + 71
37 (p)		2 (mod 5)	65	
43 (p)			59 (p)	43 + 59
49	0 (mod 7)		53 (p)	

- $n = 96$  ( $GC : 7, 13, 17, 23, 29, 37, 43$ )

$$n = 2^5 \cdot 3.$$

$$n/2 = 48.$$

$7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.

$$n \equiv 1 \pmod{5}, n \equiv 5 \pmod{7}.$$

5 (p)	0 (mod 5)	5 (mod 7)	91	
11 (p)		1 (mod 5)	85	
17 (p)			79 (p)	17 + 79
23 (p)			73 (p)	23 + 73
29 (p)			67 (p)	29 + 67
35	0 (mod 5) and 0 (mod 7)		61 (p)	
41 (p)		1 (mod 5)	55	
47 (p)		5 (mod 7)	49	
7 (p)	0 (mod 7)		89 (p)	
13 (p)			83 (p)	13 + 83
19 (p)		5 (mod 7)	77	
25	0 (mod 5)		71 (p)	
31 (p)		1 (mod 5)	65	
37 (p)			59 (p)	37 + 59
43 (p)			53 (p)	43 + 53

- $n = 90$  (GC : 7, 11, 17, 19, 23, 29, 31, 37, 43)

$$n = 2 \cdot 3^2 \cdot 5.$$

$$n/2 = 45.$$

$7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.

$$n \equiv 0 \pmod{5}, n \equiv 6 \pmod{7}.$$

5 (p)	0 (mod 5)		85	
11 (p)			79 (p)	11 + 79
17 (p)			73 (p)	17 + 73
23 (p)			67 (p)	23 + 67
29 (p)			61 (p)	29 + 61
35	0 (mod 5) and 0 (mod 7)		55	
41 (p)		6 (mod 7)	49	
7 (p)	0 (mod 7)		83 (p)	
13 (p)		6 (mod 7)	77	
19 (p)			71 (p)	19 + 71
25	0 (mod 5)		65	
31 (p)			59 (p)	31 + 59
37 (p)			53 (p)	37 + 53
43 (p)			47 (p)	43 + 47

- $n = 84$  (GC : 5, 11, 13, 17, 23, 31, 37, 41)

$$n = 2^2 \cdot 3 \cdot 7.$$

$$n/2 = 42.$$

$7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.

$$n \equiv 4 \pmod{5}, n \equiv 0 \pmod{7}.$$

5 (p)	0 (mod 5)		79 (p)	
11 (p)			73 (p)	11 + 73
17 (p)			67 (p)	17 + 67
23 (p)			61 (p)	23 + 61
29 (p)		4 (mod 5)	55	
35	0 (mod 5) and 0 (mod 7)		49	
41 (p)			43 (p)	41 + 43
7 (p)	0 (mod 7)		77	
13 (p)			71 (p)	13 + 71
19 (p)		4 (mod 5)	65	
25	0 (mod 5)		59 (p)	
31 (p)			53 (p)	31 + 53
37 (p)			47 (p)	37 + 47

- $n = 78$  ( $GC : 5, 7, 11, 17, 19, 31, 37$ )  
 $n = 2 \cdot 3 \cdot 13$ .  
 $n/2 = 39$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 1 \pmod{7}$ .

5 (p)	0 (mod 5)		73 (p)	
11 (p)			67 (p)	11 + 67
17 (p)			61 (p)	17 + 61
23 (p)		3 (mod 5)	55	
29 (p)		1 (mod 7)	49	
35	0 (mod 5) and 0 (mod 7)		43 (p)	
7 (p)	0 (mod 7)		71 (p)	
13 (p)		3 (mod 5)	65	
19 (p)			59 (p)	19 + 59
25	0 (mod 5)		53 (p)	
31 (p)			47 (p)	31 + 47
37 (p)			41 (p)	37 + 41

- $n = 72$  ( $GC : 5, 11, 13, 19, 29, 31$ )  
 $n = 2^3 \cdot 3^2$ .  
 $n/2 = 36$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 2 \pmod{5}, n \equiv 2 \pmod{7}$ .

5 (p)	0 (mod 5)		67 (p)	
11 (p)			61 (p)	11 + 61
17 (p)		2 (mod 5)	55	
23 (p)		2 (mod 7)	49	
29 (p)			43 (p)	29 + 43
35	0 (mod 5) and 0 (mod 7)		37 (p)	
7 (p)	0 (mod 7)	2 (mod 5)	65	
13 (p)			59 (p)	13 + 59
19 (p)			53 (p)	19 + 53
25	0 (mod 5)		47 (p)	
31 (p)			41 (p)	31 + 41

- $n = 66$  ( $GC : 5, 7, 13, 19, 23, 29$ )  
 $n = 2 \cdot 3 \cdot 11$ .  
 $n/2 = 33$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 1 \pmod{5}, n \equiv 3 \pmod{7}$ .

5 (p)	0 (mod 5)		61 (p)	
11 (p)		1 (mod 5)	55	
17 (p)		3 (mod 7)	49	
23 (p)			43 (p)	23 + 43
29 (p)			37 (p)	29 + 37
7 (p)	0 (mod 7)		59 (p)	
13 (p)			53 (p)	13 + 53
19 (p)			47 (p)	19 + 47
25	0 (mod 5)		41 (p)	
31 (p)		1 (mod 5) and 3 (mod 7)	35	

- $n = 60$  ( $GC : 7, 13, 17, 19, 23, 29$ )  
 $n = 2^2 \cdot 3 \cdot 5$ .  
 $n/2 = 30$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 4 \pmod{7}$ .

5 (p)	0 (mod 5)		55	
11 (p)		4 (mod 7)	49	
17 (p)			43 (p)	17 + 43
23 (p)			37 (p)	23 + 37
29 (p)			31 (p)	29 + 31
7 (p)	0 (mod 7)		53 (p)	
13 (p)			47 (p)	13 + 47
19 (p)			41 (p)	19 + 41
25	0 (mod 5)	4 (mod 7)	35	

- $n = 54$  ( $DG : 7, 11, 13, 17, 23$ )  
 $n = 2 \cdot 3^3$ .  
 $n/2 = 27$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 4 \pmod{5}, n \equiv 5 \pmod{7}$ .

5 (p)	0 (mod 5)	5 (mod 7)	49	
11 (p)			43 (p)	11 + 43
17 (p)			37 (p)	17 + 37
23 (p)			31 (p)	23 + 31
7 (p)	0 (mod 7)		47 (p)	
13 (p)			41 (p)	13 + 41
19 (p)		4 (mod 5) and 5 (mod 7)	35	
25	0 (mod 5)		29	

- $n = 48$  ( $GC : 5, 7, 11, 17, 19$ )  
 $n = 2^4 \cdot 3$ .  
 $n/2 = 24$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 3 \pmod{5}$ .

5 (p)	0 (mod 5)		43 (p)	
11 (p)			37 (p)	11 + 37
17 (p)			31 (p)	17 + 31
23 (p)		3 (mod 5)	25	
7 (p)			41 (p)	7 + 41
13 (p)		3 (mod 5)	35	
19 (p)			29 (p)	19 + 29

- $n = 42$  ( $GC : 5, 11, 13, 19$ )  
 $n = 2 \cdot 3 \cdot 7$ .  
 $n/2 = 21$ .  
 $5 < \sqrt{n} < 5$ . The modulus to be considered is 5.  
 $n \equiv 2 \pmod{5}$ .

5 (p)	0 (mod 5)		37 (p)	
11 (p)			31 (p)	11 + 31
17 (p)		2 (mod 5)	25	
7 (p)		2 (mod 5)	35	
13 (p)			29 (p)	13 + 29
19 (p)			23 (p)	19 + 23



- $n = 36$  (GC : 5, 7, 13, 17)  
 $n = 2^2 \cdot 3^2$ .  
 $n/2 = 18$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 1 \pmod{5}$ .

5 (p)	0 (mod 5)		31 (p)	
11 (p)		1 (mod 5)	25	
17 (p)			19 (p)	17 + 19
7 (p)			29 (p)	7 + 29
13 (p)			23 (p)	13 + 23

- $n = 30$  (GC : 7, 11, 13)  
 $n = 2 \cdot 3 \cdot 5$ .  
 $n/2 = 15$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 0 \pmod{5}$ .

5 (p)	0 (mod 5)	25	
11 (p)		19 (p)	11 + 19
7 (p)		23 (p)	7 + 23
13 (p)		17 (p)	13 + 17

## 2 Even numbers of the form $n = 6m + 4$ from 142 to 28

The double sieve of Eratosthenes application is presented in a table containing only  $\left\lfloor \frac{n+6}{12} \right\rfloor$  numbers belonging to the arithmetic progression  $6k - 1$ .

- $n = 142$  (GC : 3, 5, 11, 29, 41, 53, 59, 71)  
 $n = 2 \cdot 71$ .  
 $n/2 = 71$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 2 \pmod{5}, n \equiv 2 \pmod{7}, n \equiv 10 \pmod{11}$ .

5 (p)	0 (mod 5)		137 (p)	
11 (p)	0 (mod 11)		131 (p)	
17 (p)		2 (mod 5)	125	
23 (p)		2 (mod 7)	119	
29 (p)			113 (p)	29 + 113
35	0 (mod 5) and 0 (mod 7)		107 (p)	
41 (p)			101 (p)	41 + 101
47 (p)		2 (mod 5)	95	
53 (p)			89 (p)	53 + 89
59 (p)			83 (p)	59 + 83
65	0 (mod 5)	2 (mod 7) et 10 (mod 11)	77	
71 (p)			71 (p)	71 + 71

- $n = 136$  (GC : 5, 23, 29, 47, 53)  
 $n = 2^3 \cdot 17$ .  
 $n/2 = 68$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 1 \pmod{5}, n \equiv 3 \pmod{7}, n \equiv 4 \pmod{11}$ .

5 (p)	0 (mod 5)		131 (p)	
11 (p)	0 (mod 11)	1 (mod 5)	125	
17 (p)		3 (mod 7)	119	
23 (p)			113 (p)	23 + 113
29 (p)			107 (p)	29 + 107
35	0 (mod 5) and 0 (mod 7)		101 (p)	
41 (p)		1 (mod 5)	95	
47 (p)			89 (p)	47 + 89
53 (p)			83 (p)	53 + 83
59 (p)		3 (mod 7) et 4 (mod 11)	77	
65	0 (mod 5)		71 (p)	

- $n = 130$  (GC : 3, 17, 23, 29, 41, 47, 59)  
 $n = 2 \cdot 5 \cdot 13$ .  
 $n/2 = 65$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 0 \pmod{5}, n \equiv 4 \pmod{7}, n \equiv 9 \pmod{11}$ .

5 (p)	0 (mod 5)		125	
11 (p)	0 (mod 11)	4 (mod 7)	119	
17 (p)			113 (p)	17 + 113
23 (p)			107 (p)	23 + 107
29 (p)			101 (p)	29 + 101
35	0 (mod 5) and 0 (mod 7)		95	
41 (p)			89 (p)	41 + 89
47 (p)			83 (p)	47 + 83
53 (p)		4 (mod 7) et 9 (mod 11)	77	
59 (p)			71 (p)	59 + 71
65	0 (mod 5)		65	

- $n = 124$  (GC : 11, 17, 23, 41, 53)  
 $n = 2^2 \cdot 31$ .  
 $n/2 = 62$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 4 \pmod{5}, n \equiv 5 \pmod{7}, n \equiv 3 \pmod{11}$ .

5 (p)	0 (mod 5)	5 (mod 7)	119	
11 (p)	0 (mod 11)		113 (p)	
17 (p)			107 (p)	17 + 107
23 (p)			101 (p)	23 + 101
29 (p)		4 (mod 5)	95	
35	0 (mod 5) and 0 (mod 7)		89 (p)	
41 (p)			83 (p)	41 + 83
47 (p)		5 (mod 7) et 3 (mod 11)	77	
53 (p)			71 (p)	53 + 71
59 (p)		4 (mod 5)	65	

- $n = 118$  ( $GC : 5, 11, 17, 29, 47, 59$ )  
 $n = 2 \cdot 59$ .  
 $n/2 = 59$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 6 \pmod{7}$ .

5 (p)	0 (mod 5)		113 (p)	
11 (p)			107 (p)	11 + 107
17 (p)			101 (p)	17 + 101
23 (p)		3 (mod 5)	95	
29 (p)			89 (p)	29 + 89
35	0 (mod 5) and 0 (mod 7)		83 (p)	
41 (p)		6 (mod 7)	77	
47 (p)			71 (p)	47 + 71
53 (p)		3 (mod 5)	65	
59 (p)			59 (p)	59 + 59

- $n = 112$  ( $DG : 3, 5, 11, 23, 29, 41, 53$ )  
 $n = 2^4 \cdot 7$ .  
 $n/2 = 56$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 2 \pmod{5}, n \equiv 0 \pmod{7}$ .

5 (p)	0 (mod 5)		107 (p)	
11 (p)			101 (p)	11 + 101
17 (p)		2 (mod 5)	95	
23 (p)			89 (p)	23 + 89
29 (p)			83 (p)	29 + 83
35	0 (mod 5) and 0 (mod 7)		77	
41 (p)			71 (p)	41 + 71
47 (p)		2 (mod 5)	65	
53 (p)			59 (p)	53 + 59

- $n = 106$  ( $GC : 3, 5, 17, 23, 47, 53$ )  
 $n = 2 \cdot 53$ .  
 $n/2 = 53$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 1 \pmod{5}, n \equiv 1 \pmod{7}$ .

5 (p)	0 (mod 5)		101 (p)	
11 (p)		1 (mod 5)	95	
17 (p)			89 (p)	17 + 89
23 (p)			83 (p)	23 + 83
29 (p)		1 (mod 7)	77	
35	0 (mod 5) et 0 (mod 7)		71 (p)	
41 (p)		1 (mod 5)	65	
47 (p)			59 (p)	47 + 59
53 (p)			53 (p)	53 + 53

- $n = 100$  ( $GC : 3, 11, 17, 29, 41, 47$ )  
 $n = 2^2 \cdot 5^2$ .  
 $n/2 = 50$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 2 \pmod{7}$ .

5 (p)	0 (mod 5)		95	
11 (p)			89 (p)	11 + 89
17 (p)			83 (p)	17 + 83
23 (p)		2 (mod 7)	77	
29 (p)			71 (p)	29 + 71
35	0 (mod 5) et 0 (mod 7)		65	
41 (p)			59 (p)	41 + 59
47 (p)			53 (p)	47 + 53

- $n = 94$  ( $GC : 5, 11, 23, 41, 47$ )  
 $n = 2 \cdot 47$ .  
 $n/2 = 47$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 4 \pmod{5}, n \equiv 3 \pmod{7}$ .

5 (p)	0 (mod 5)		89 (p)	
11 (p)			83 (p)	11 + 83
17 (p)		3 (mod 7)	77	
23 (p)			71 (p)	23 + 71
29 (p)		4 (mod 5)	65	
35	0 (mod 5) et 0 (mod 7)		59 (p)	
41 (p)			53 (p)	41 + 53
47 (p)			47 (p)	47 + 47

- $n = 88$  ( $DG : 5, 17, 29, 41$ )  
 $n = 2^3 \cdot 11$ .  
 $n/2 = 44$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 4 \pmod{7}$ .

5 (p)	0 (mod 5)		83 (p)	
11 (p)		4 (mod 7)	77	
17 (p)			71 (p)	17 + 71
23 (p)		3 (mod 5)	65	
29 (p)			59 (p)	29 + 59
35	0 (mod 5) et 0 (mod 7)		53 (p)	
41 (p)			47 (p)	41 + 47

- $n = 82$  ( $GC : 3, 11, 23, 29, 41$ )  
 $n = 2 \cdot 41$ .  
 $n/2 = 41$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 2 \pmod{5}, n \equiv 5 \pmod{7}$ .

5 (p)	0 (mod 5)	5 (mod 7)	77	
11 (p)			71 (p)	11 + 71
17 (p)		2 (mod 5)	65	
23 (p)			59 (p)	23 + 59
29 (p)			53 (p)	29 + 53
35	0 (mod 5) et 0 (mod 7)		47 (p)	
41 (p)			41 (p)	41 + 41

- $n = 76$  (GC : 3, 5, 17, 23, 29)  
 $n = 2^2 \cdot 19$ .  
 $n/2 = 38$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 1 \pmod{5}, n \equiv 6 \pmod{7}$ .

5 (p)	0 (mod 5)		71 (p)	
11 (p)		1 (mod 5)	65	
17 (p)			59 (p)	17 + 59
23 (p)			53 (p)	23 + 53
29 (p)			47 (p)	29 + 47
35	0 (mod 5) et 0 (mod 7)		41 (p)	

- $n = 70$  (GC : 3, 11, 17, 23, 29)  
 $n = 2 \cdot 5 \cdot 7$ .  
 $n/2 = 35$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 0 \pmod{7}$ .

5 (p)	0 (mod 5)		65	
11 (p)			59 (p)	11 + 59
17 (p)			53 (p)	17 + 53
23 (p)			47 (p)	23 + 47
29 (p)			41 (p)	29 + 41
35	0 (mod 5) et 0 (mod 7)		35	

- $n = 64$  (GC : 3, 5, 11, 17, 23)  
 $n = 2^6$ .  
 $n/2 = 32$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 4 \pmod{5}, n \equiv 1 \pmod{7}$ .

5 (p)	0 (mod 5)		59 (p)	
11 (p)			53 (p)	11 + 53
17 (p)			47 (p)	17 + 47
23 (p)			41 (p)	23 + 41
29 (p)		4 (mod 5) et 1 (mod 7)	35	

- $n = 58$  (GC : 5, 11, 17, 29)  
 $n = 2 \cdot 29$ .  
 $n/2 = 29$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 2 \pmod{7}$ .

5 (p)	0 (mod 5)		53 (p)	
11 (p)			47 (p)	11 + 47
17 (p)			41 (p)	17 + 41
23 (p)		3 (mod 5) et 2 (mod 7)	35	
29 (p)			29 (p)	29 + 29

- $n = 52$  ( $GC : 5, 11, 23$ )  
 $n = 2^2 \cdot 13$ .  
 $n/2 = 26$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 2 \pmod{5}, n \equiv 3 \pmod{7}$ .

5 (p)	0 (mod 5)		47 (p)	
11 (p)			41 (p)	11 + 41
17 (p)		2 (mod 5) et 3 (mod 7)	35	
23 (p)			29 (p)	23 + 29

- $n = 46$  ( $GC : 3, 5, 17, 23$ )  
 $n = 2 \cdot 23$ .  
 $n/2 = 23$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 1 \pmod{5}$ .

5 (p)	0 (mod 5)		41 (p)	
11 (p)		1 (mod 5)	35	
17 (p)			29 (p)	17 + 29
23 (p)			23 (p)	23 + 23

- $n = 40$  ( $GC : 3, 11, 17$ )  
 $n = 2^3 \cdot 5$ .  
 $n/2 = 20$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 0 \pmod{5}$ .

5 (p)	0 (mod 5)	35	
11 (p)		29 (p)	11 + 29
17 (p)		23 (p)	17 + 23

- $n = 34$  ( $GC : 3, 5, 11, 17$ )  
 $n = 2 \cdot 17$ .  
 $n/2 = 17$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 4 \pmod{5}$ .

5 (p)	0 (mod 5)	29 (p)	
11 (p)		23 (p)	11 + 23
17 (p)		17 (p)	17 + 17

- $n = 28$  ( $GC : 5, 11$ )  
 $n = 2^2 \cdot 7$ .  
 $n/2 = 14$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 3 \pmod{5}$ .

5 (p)	0 (mod 5)	23	
11 (p)		17 (p)	11 + 17

### 3 Even numbers of the form $n = 6m + 2$ from 140 to 26

The double sieve of Eratosthenes application is presented in a table containing only  $\left\lfloor \frac{n}{12} \right\rfloor$  numbers belonging to the arithmetic progression  $6k + 1$ .

- $n = 140$  (GC : 3, 13, 31, 37, 43, 61, 67)  
 $n = 2^2 \cdot 5 \cdot 7$ .  
 $n/2 = 70$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 0 \pmod{5}, n \equiv 0 \pmod{7}, n \equiv 8 \pmod{11}$ .

7 (p)	0 (mod 7)		133	
13 (p)			127 (p)	13 + 127
19 (p)		8 (mod 11)	121	
25	0 (mod 5)		115	
31 (p)			109 (p)	31 + 109
37 (p)			103 (p)	37 + 103
43 (p)			97 (p)	43 + 97
49	0 (mod 7)		91	
55	0 (mod 5) et 0 (mod 11)		85	
61 (p)			79 (p)	61 + 79
67 (p)			73 (p)	67 + 73

- $n = 134$  (GC : 3, 7, 31, 37, 61, 67)  
 $n = 2 \cdot 67$ .  
 $n/2 = 67$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 4 \pmod{5}, n \equiv 1 \pmod{7}, n \equiv 2 \pmod{11}$ .

7 (p)	0 (mod 7)		127 (p)	
13 (p)		2 (mod 11)	121	
19 (p)		4 (mod 5)	115	
25	0 (mod 5)		109 (p)	
31 (p)			103 (p)	31 + 103
37 (p)			97 (p)	37 + 97
43 (p)		1 (mod 7)	91	
49	0 (mod 7)	4 (mod 5)	85	
55	0 (mod 5) et 0 (mod 11)		79 (p)	
61 (p)			73 (p)	61 + 73
67 (p)			67 (p)	67 + 67

- $n = 128$  (GC : 19, 31, 61)  
 $n = 2^7$ .  
 $n/2 = 64$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 3 \pmod{5}, n \equiv 2 \pmod{7}, n \equiv 7 \pmod{11}$ .

7 (p)	0 (mod 7)	7 (mod 11)	121	
13 (p)		3 (mod 5)	115	
19 (p)			109 (p)	19 + 109
25	0 (mod 5)		103 (p)	
31 (p)			97 (p)	31 + 97
37 (p)		2 (mod 7)	93	
43 (p)		3 (mod 5)	87	
49	0 (mod 7)		81	
55	0 (mod 5) et 0 (mod 11)		75	
61			69 (p)	61 + 69

- $n = 122$  ( $GC : 13, 19, 43, 61$ )  
 $n = 2 \cdot 61$ .  
 $n/2 = 61$ .  
 $11 < \sqrt{n} < 13$ . The moduli to be considered are 5, 7 and 11.  
 $n \equiv 2 \pmod{5}, n \equiv 3 \pmod{7}, n \equiv 1 \pmod{11}$ .

7 (p)	0 (mod 7)	2 (mod 5)	115	
13 (p)			109 (p)	13 + 109
19 (p)			103 (p)	19 + 103
25	0 (mod 5)		97 (p)	
31 (p)		3 (mod 7)	91	
37 (p)		2 (mod 5)	85	
43 (p)			79 (p)	43 + 79
49	0 (mod 7)		73 (p)	
55	0 (mod 5)		67 (p)	
61 (p)			61 (p)	61 + 61

- $n = 116$  ( $GC : 3, 7, 13, 19, 37, 43$ )  
 $n = 2^2 \cdot 29$ .  
 $n/2 = 58$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 1 \pmod{5}, n \equiv 4 \pmod{7}$ .

7 (p)	0 (mod 7)		109 (p)	
13 (p)			103 (p)	13 + 103
19 (p)			97 (p)	19 + 97
25	0 (mod 5)	4 (mod 7)	91	
31 (p)		1 (mod 5)	85	
37 (p)			79 (p)	37 + 79
43 (p)			73 (p)	43 + 73
49	0 (mod 7)		67	
55	0 (mod 5) et 0 (mod 11)		61 (p)	

- $n = 110$  ( $GC : 3, 7, 13, 31, 37, 43$ )  
 $n = 2 \cdot 5 \cdot 11$ .  
 $n/2 = 55$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 5 \pmod{7}$ .

7 (p)	0 (mod 7)		103 (p)	
13 (p)			97 (p)	13 + 97
19 (p)		5 (mod 7)	91	
25	0 (mod 5)		85	
31 (p)			79 (p)	31 + 79
37 (p)			73 (p)	37 + 73
43 (p)			67 (p)	43 + 67
49	0 (mod 7)		61 (p)	
55	0 (mod 5) et 0 (mod 11)		55	



- $n = 104$  (GC : 3, 7, 31, 37, 43)  
 $n = 2^3 \cdot 13$ .  
 $n/2 = 52$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 4 \pmod{5}, n \equiv 6 \pmod{7}$ .

7 (p)	0 (mod 7)		97 (p)	
13 (p)		6 (mod 7)	91	
19 (p)		4 (mod 5)	85	
25	0 (mod 5)		79 (p)	
31 (p)			73 (p)	31 + 73
37 (p)			67 (p)	37 + 67
43 (p)			61 (p)	43 + 61
49	0 (mod 7)	4 (mod 5)	55	

- $n = 98$  (GC : 19, 31, 37)  
 $n = 2 \cdot 7^2$ .  
 $n/2 = 49$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 0 \pmod{7}$ .

7 (p)	0 (mod 7)		91	
13 (p)		3 (mod 5)	85	
19 (p)			79 (p)	19 + 79
25	0 (mod 5)		73	
31 (p)			67 (p)	31 + 67
37 (p)			61 (p)	37 + 61
43 (p)		3 (mod 5)	55	
49	0 (mod 7)		49	

- $n = 92$  (GC : 3, 13, 19, 31)  
 $n = 2^2 \cdot 23$ .  
 $n/2 = 46$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 2 \pmod{5}, n \equiv 1 \pmod{7}$ .

7 (p)	0 (mod 7)	2 (mod 5)	87	
13 (p)			81 (p)	13 + 81
19 (p)			75 (p)	19 + 75
25	0 (mod 5)		69	
31 (p)			63 (p)	31 + 63
37 (p)		2 (mod 5)	57 (p)	
43 (p)		1 (mod 7)	51	

- $n = 86$  (GC : 3, 7, 13, 19, 43)  
 $n = 2 \cdot 43$ .  
 $n/2 = 43$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 1 \pmod{5}, n \equiv 2 \pmod{7}$ .

7 (p)	0 (mod 7)		79 (p)	
13 (p)			73 (p)	13 + 73
19 (p)			67 (p)	19 + 67
25	0 (mod 5)		61 (p)	
31 (p)		1 (mod 5)	55	
37 (p)		2 (mod 7)	49	
43 (p)			43 (p)	43 + 43

- $n = 80$  ( $GC : 7, 13, 19, 37$ )  
 $n = 2^4 \cdot 5$ .  
 $n/2 = 40$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 3 \pmod{7}$ .

7 (p)	0 (mod 7)		73 (p)	
13 (p)			67 (p)	13 + 67
19 (p)			61 (p)	19 + 61
25	0 (mod 5)		55	
31 (p)		3 (mod 7)	49	
37 (p)			43 (p)	37 + 43

- $n = 74$  ( $GC : 3, 7, 13, 31, 37$ )  
 $n = 2 \cdot 37$ .  
 $n/2 = 37$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 4 \pmod{5}, n \equiv 4 \pmod{7}$ .

7 (p)	0 (mod 7)		67 (p)	
13 (p)			61 (p)	13 + 61
19 (p)		4 (mod 5)	55	
25	0 (mod 5)	4 (mod 7)	49	
31 (p)			43 (p)	31 + 43
37 (p)			37 (p)	37 + 37

- $n = 68$  ( $GC : 7, 31$ )  
 $n = 2^2 \cdot 17$ .  
 $n/2 = 34$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 3 \pmod{5}, n \equiv 5 \pmod{7}$ .

7 (p)	0 (mod 7)		61 (p)	
13 (p)		3 (mod 5)	55	
19 (p)		5 (mod 7)	49	
25	0 (mod 5)		43 (p)	
31 (p)			37 (p)	31 + 37

- $n = 62$  ( $GC : 3, 19, 31$ )  
 $n = 2 \cdot 31$ .  
 $n/2 = 31$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 2 \pmod{5}, n \equiv 6 \pmod{7}$ .

7 (p)	0 (mod 7)	2 (mod 5)	55	
13 (p)		6 (mod 7)	49	
19 (p)			43 (p)	19 + 43
25	0 (mod 5)		37 (p)	
31 (p)			31 (p)	31 + 31

- $n = 56$  (GC : 3, 13, 19)  
 $n = 2^3 \cdot 7$ .  
 $n/2 = 28$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 1 \pmod{5}, n \equiv 0 \pmod{7}$ .

7 (p)	0 (mod 7)	49	
13 (p)		43 (p)	13 + 43
19 (p)		37 (p)	19 + 37
25	0 (mod 5)	31	

- $n = 50$  (GC : 3, 7, 13, 19)  
 $n = 2 \cdot 5^2$ .  
 $n/2 = 25$ .  
 $7 < \sqrt{n} < 11$ . The moduli to be considered are 5 and 7.  
 $n \equiv 0 \pmod{5}, n \equiv 1 \pmod{7}$ .

7 (p)	0 (mod 7)	43 (p)	
13 (p)		37 (p)	13 + 37
19 (p)		31 (p)	19 + 31
25	0 (mod 5)	25	

- $n = 44$  (GC : 3, 7, 13)  
 $n = 2^2 \cdot 11$ .  
 $n/2 = 22$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 4 \pmod{5}$ .

7 (p)		37 (p)	
13 (p)		31 (p)	13 + 31
19 (p)	4 (mod 5)	25	

- $n = 38$  (GC : 7, 19)  
 $n = 2 \cdot 19$ .  
 $n/2 = 19$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 3 \pmod{5}$ .

7 (p)		31 (p)	
13 (p)	3 (mod 5)	25	
19		19 (p)	19 + 19

- $n = 32$  (GC : 3, 13)  
 $n = 2^5$ .  
 $n/2 = 16$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 2 \pmod{5}$ .

7 (p)	2 (mod 5)	25	
13		19 (p)	13 + 19

- $n = 26$  (GC : 3, 7, 13)  
 $n = 2 \cdot 13$ .  
 $n/2 = 13$ .  
 $5 < \sqrt{n} < 7$ . The modulus to be considered is 5.  
 $n \equiv 1 \pmod{5}$ .

7 (p)		19 (p)	
13		13 (p)	13 + 13